



# Estimating Load Condition Having Caused Structure Failure and an Optimal Design Taking Account of the Estimated Result

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# Introduction

[ What to optimize ]



Crane-hook

←  
close-up



Excavators having a crane-hook can do both **digging** and **suspension** work.



# Background

Contrary to its convenience, crane-hook is damaged during some kind of suspension works.

typical crane-hook



failed sample



It is necessary to take effective steps.



Real conditions are **unclear...**



# Policy

★ Improvement of performance

**(A) Identification of applied load condition**

**(B) Shape design of crane-hook**

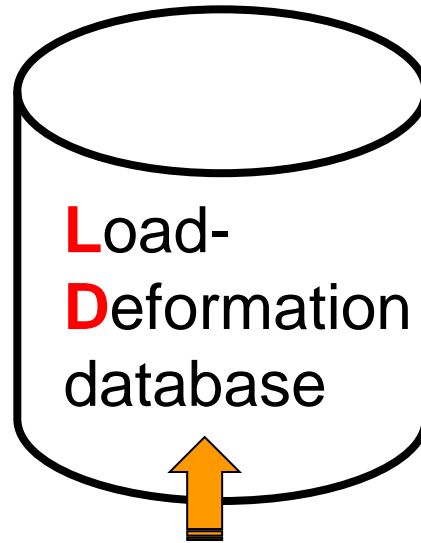
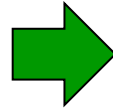
- load applied point, direction, magnitude
- probability distribution of critical load

- light weight
- strength to critical load condition

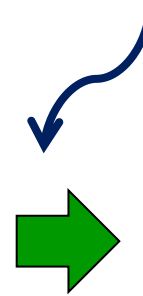
# Previous Study

Our previous work (REC2010)

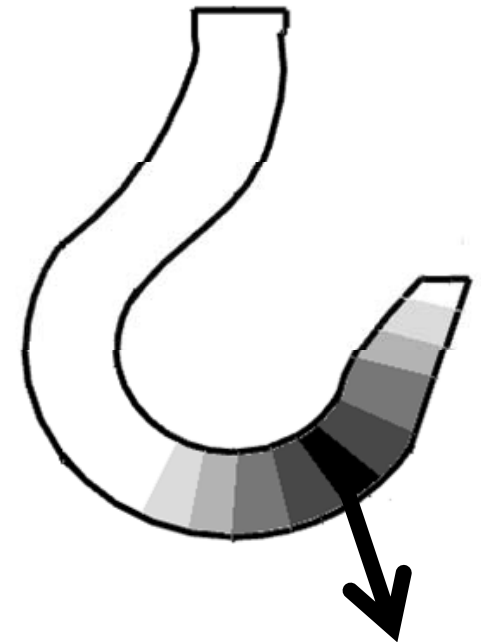
failed sample



**Bayesian theory**



estimation results



Analysis results  
based on linear elastic FEM model

# Current Study

## □ Introduction of elasto-plastic analysis

identification of **load applied point**  
**load direction**

} previous work

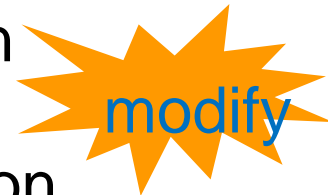
**+** **load magnitude**



## □ Support for multi peak distribution model

Estimation result is obtained based on

**single peak** probability distribution function

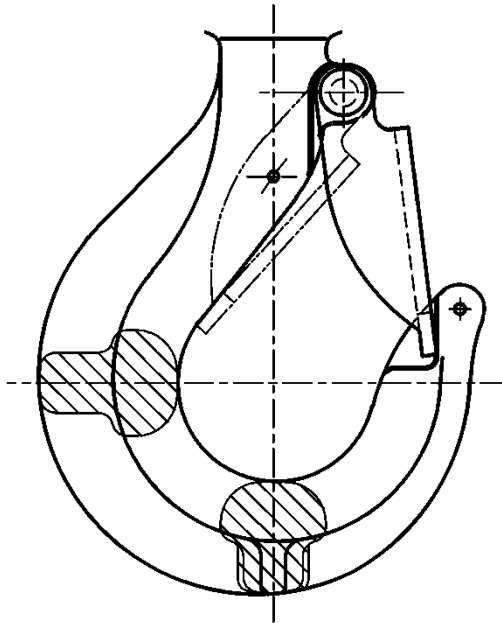


↳ **multi peak** probability distribution function

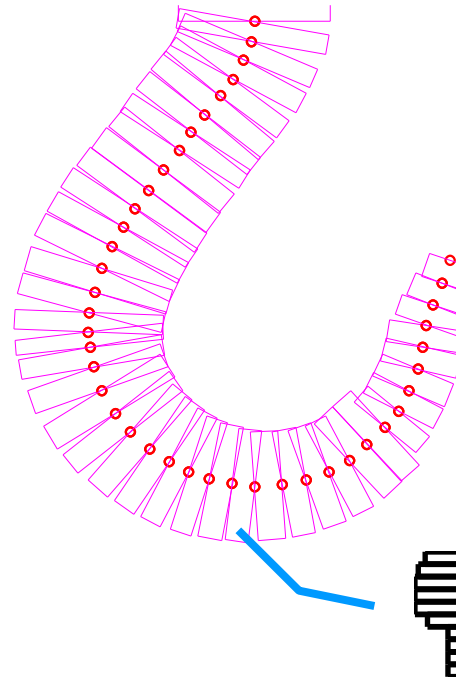
↪ **EM algorithm**

# Crane-Hook Model

design drawing



adopted FEM model



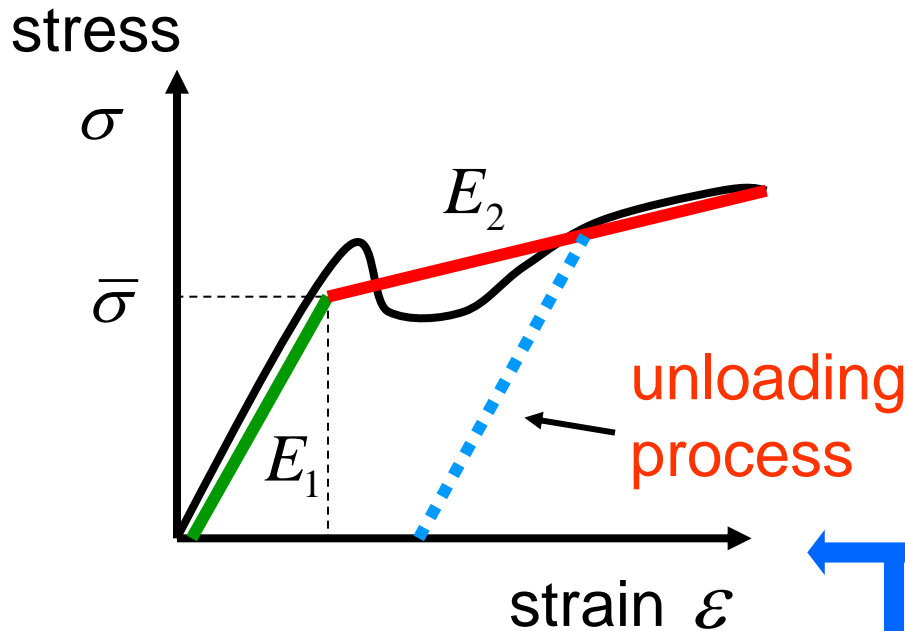
\*Latch part is omitted.

cross-sectional shape

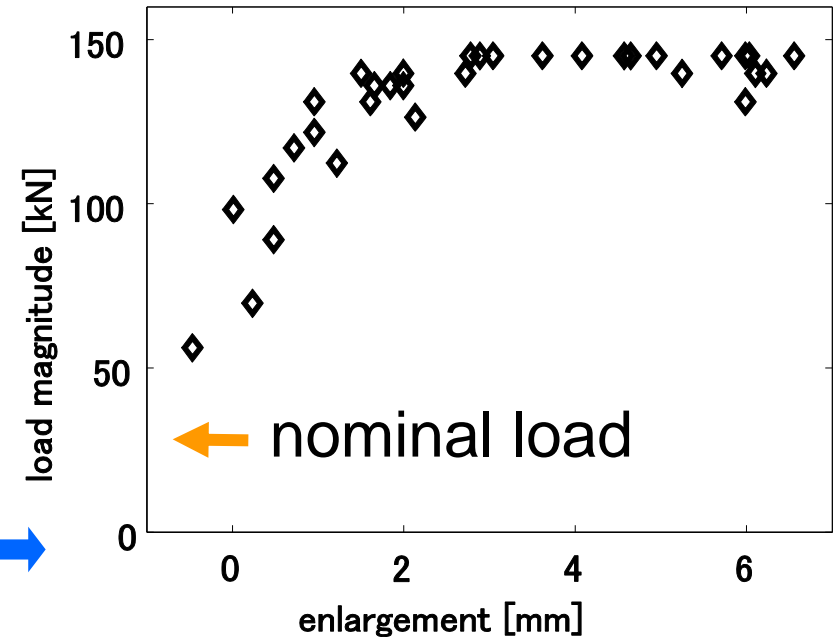
- FEM model is constructed by  $N_e$  beam elements.
- Each element is constructed by  $N_d$  layers.

# Stress-Strain Relationship

adopted bi-linear model



experimental result



yield stress

$$\bar{\sigma}^* = 200 \text{ [MPa]}$$

Young's modulus

$$E_1^* = 260 \text{ [GPa]}$$

tangent modulus

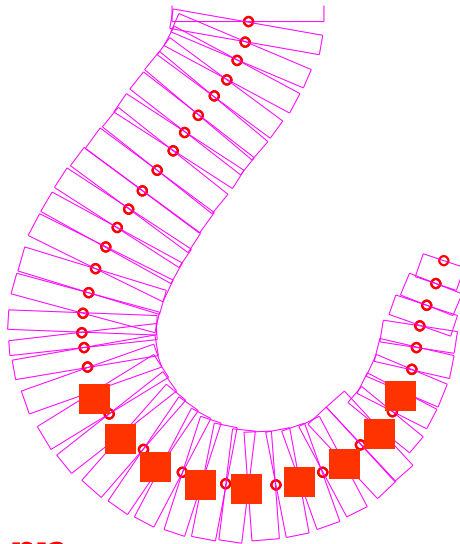
$$E_2^* = 1 \text{ [GPa]}$$



# Load Condition

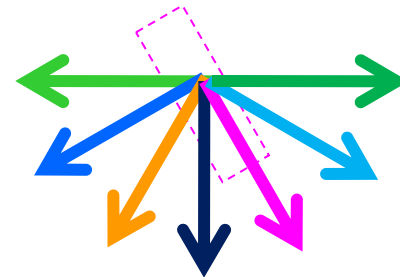
## applied load condition on FEM model

(1) load applied point



**9 pattern**

(2) load direction



**7 pattern**

(3) load magnitude

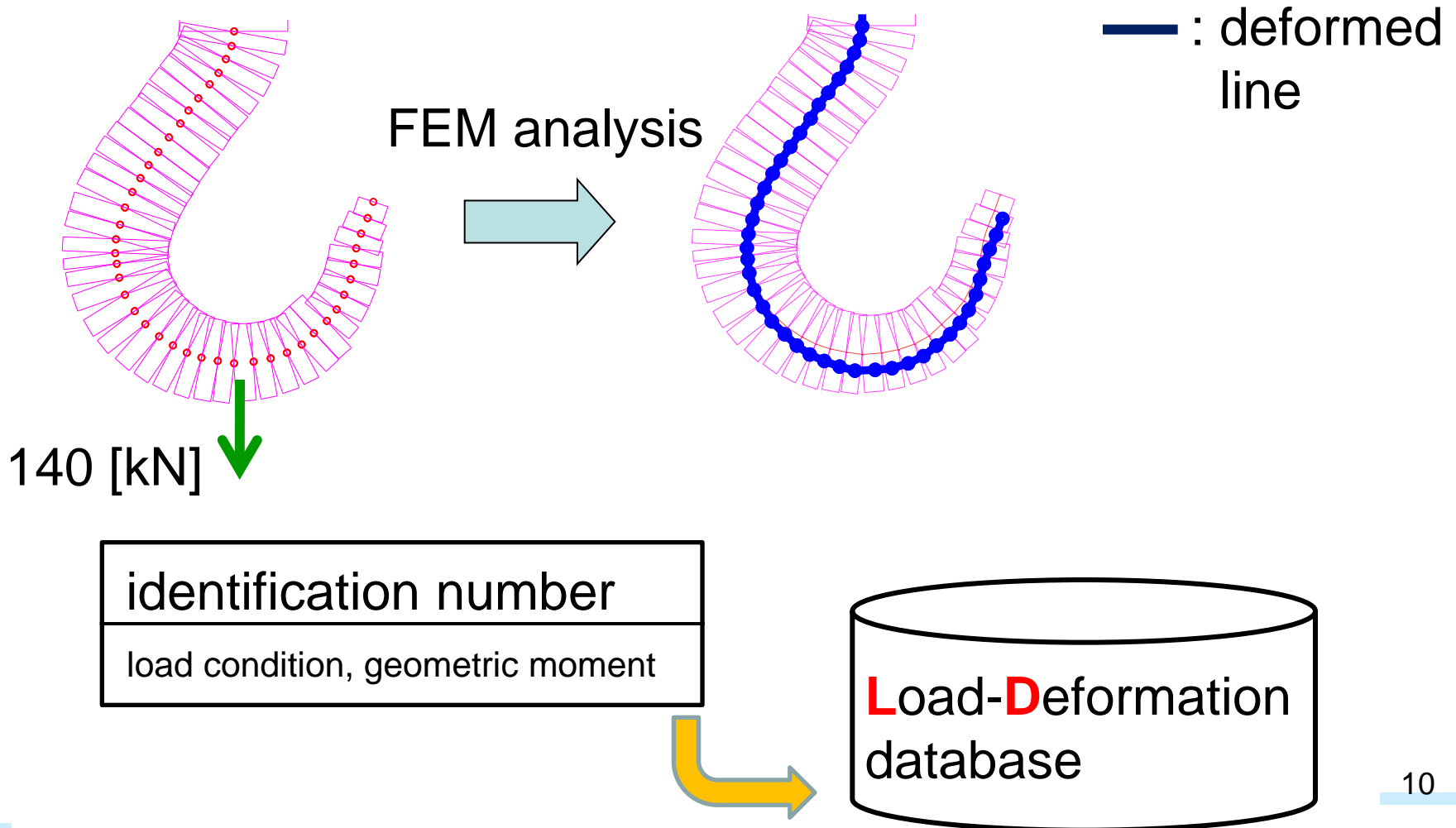
**20kN, 40kN, 60kN, 80kN**

**100kN, 120kN, 140kN**

**7 pattern**

all combination: **441 pattern**

# Construction of Database

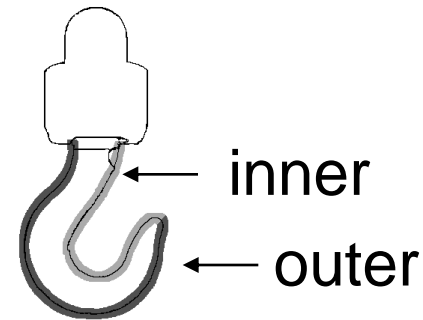


# Feature Extraction

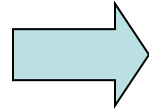
failed sample



outline of hook



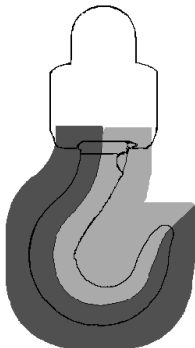
edge detection



dilation

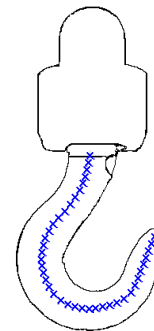
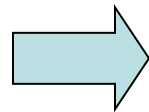


boundary of inner and outer



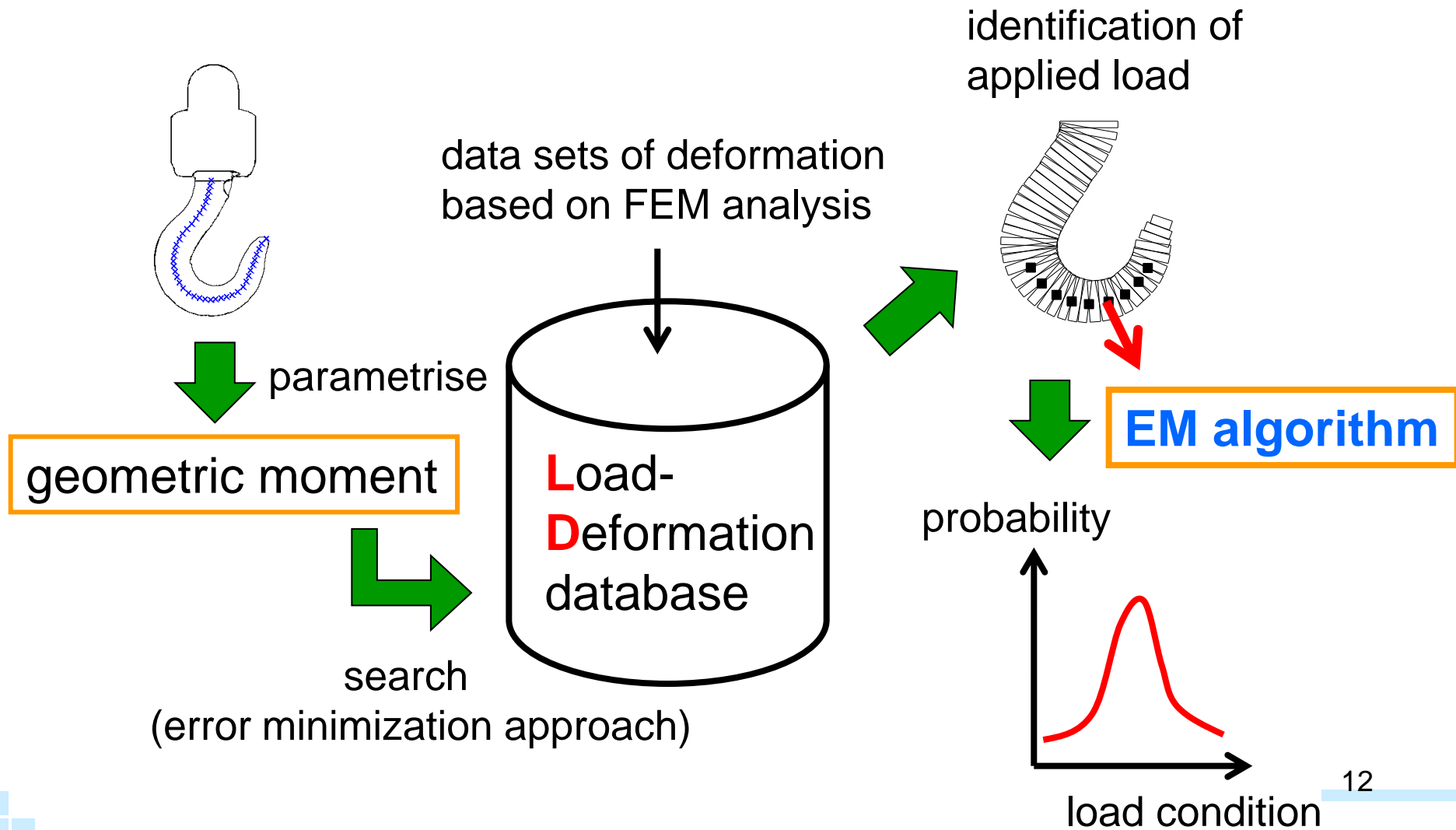
extracted feature points

division



× : feature point

# Estimation Process



# EM Algorithm

## EM (Expectation Maximization)

- iterative optimization method to estimate unknown parameters
- maximize posterior probability

$\Theta$  : some unknown parameters

$G$  : some “hidden” nuisance variables

$\chi$  : given measurement data

search for a maximum of  $P(\Theta, G | \chi)$

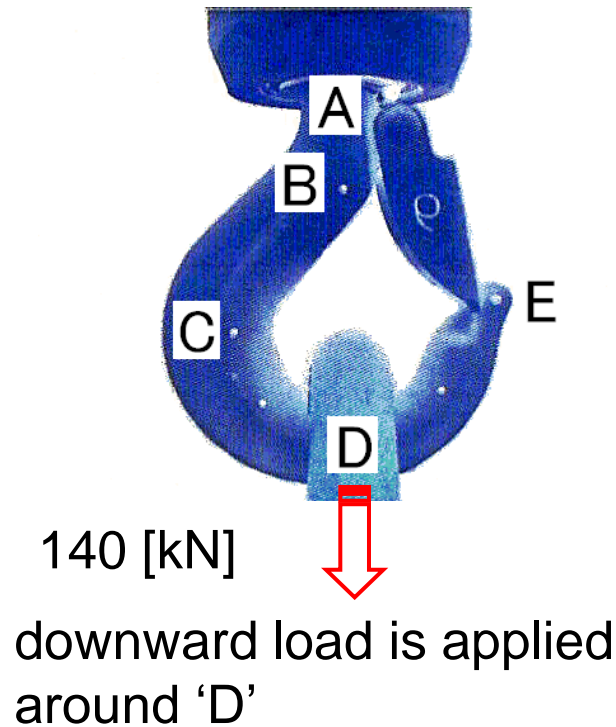
1. **step E**: calculate  $P(\Theta^{\text{old}}, G | \chi)$

2. **step M**:

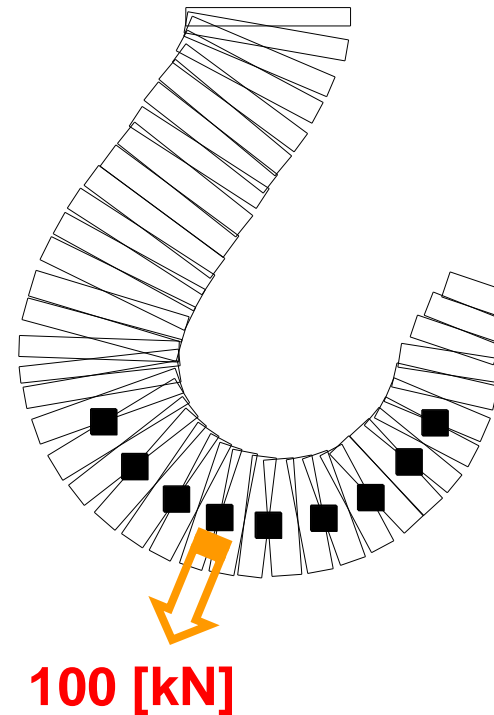
$$\Theta^{\text{new}} = \arg \max_{\Theta} \sum_G P(\Theta^{\text{old}}, G | \chi) \ln P(\Theta, G | \chi)$$

# Applicability Test

- load identification using stretch experiment image



estimation result



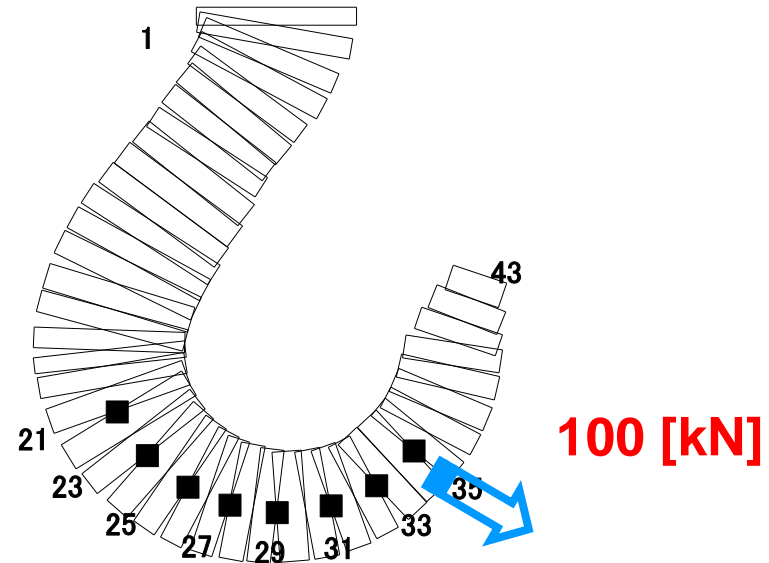
- ★ estimated load magnitude is smaller than actual load
- ★ the estimation method has uncertainty to this level

# Sample Result

failed hook



identification result

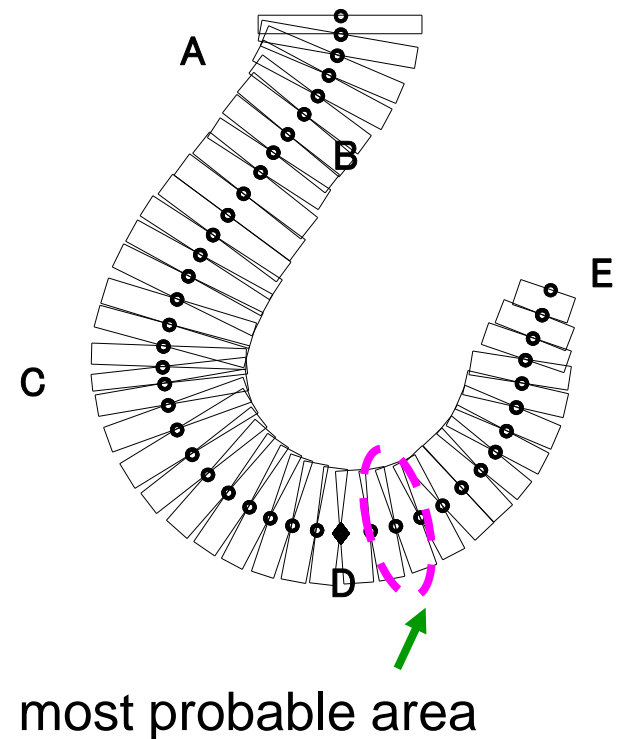
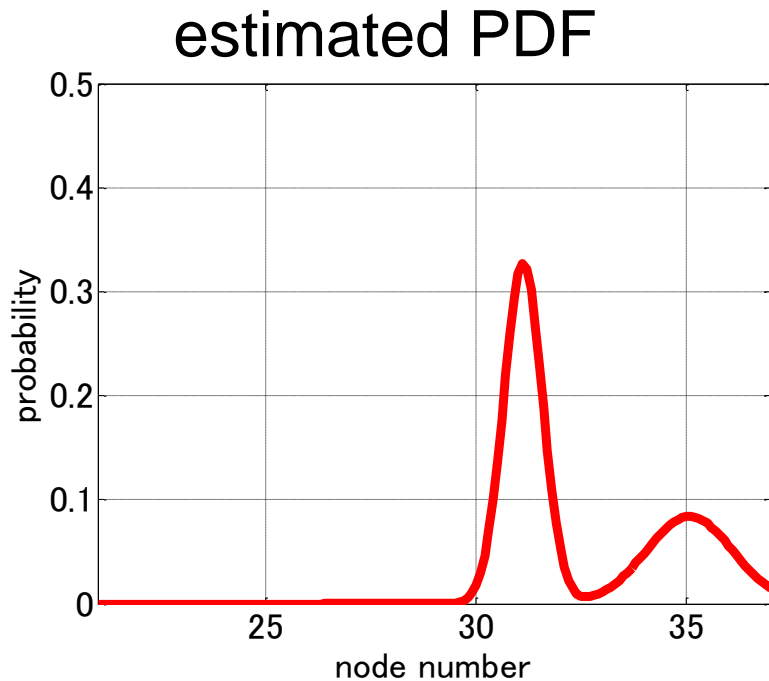


- load applied position shifts **rightward** from lower center
- load magnitude is **3 times** greater than nominal load
- load direction shifts **rightward**

# Estimation Result (1/2)

We apply the method to 12 failed samples.

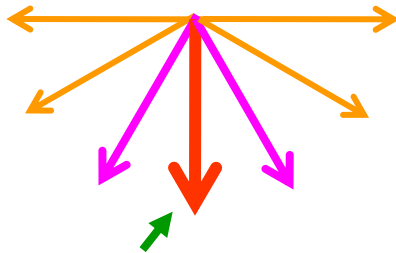
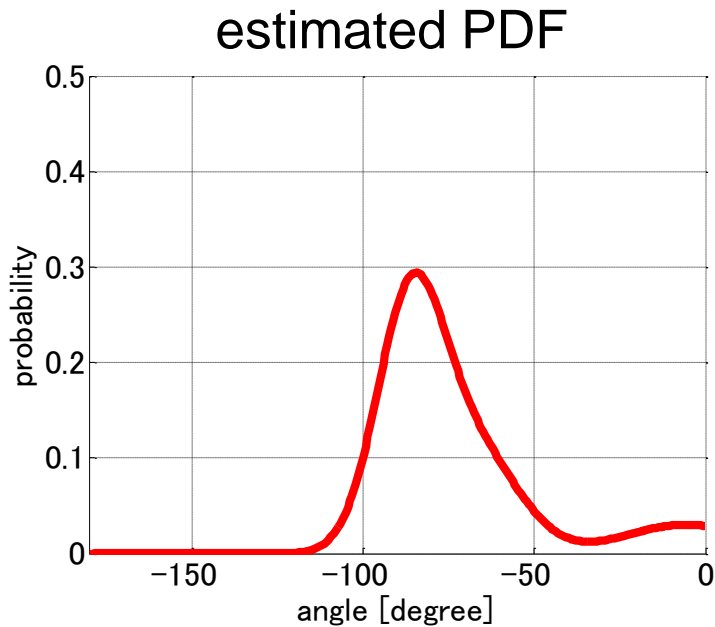
★ load applied point





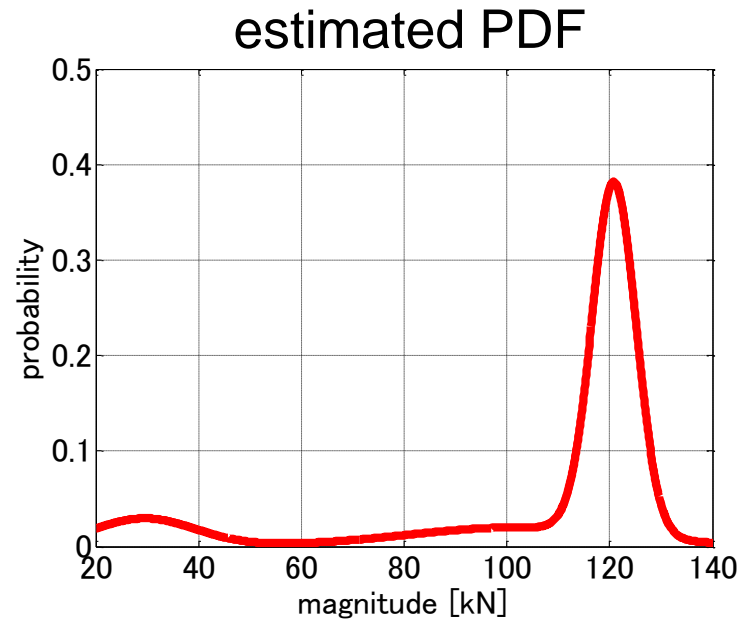
# Estimation Result (2/2)

## ★ load direction



most probable direction

## ★ load magnitude



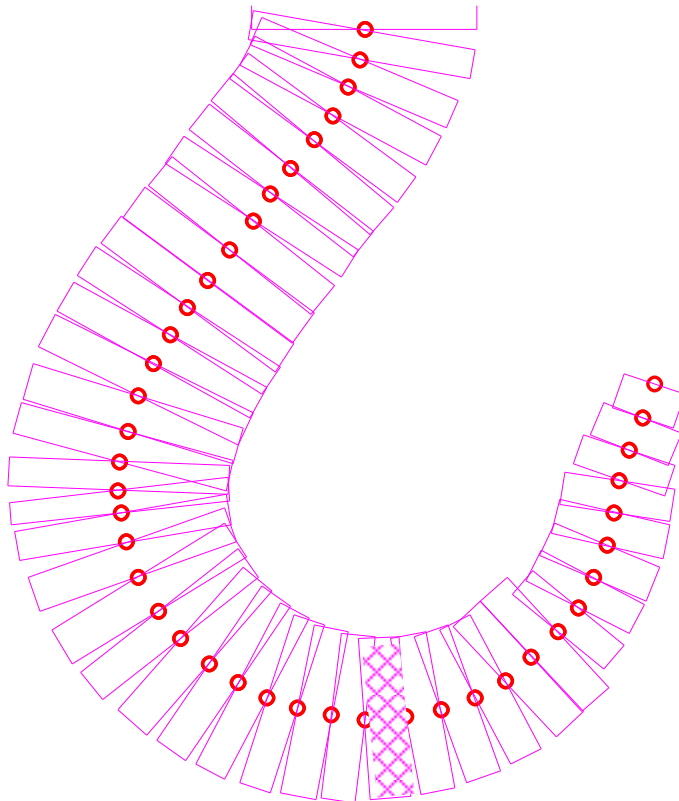
peak is at **120 [kN]**

(nominal load is 29 [kN])

# FEM model

## Shape design of crane-hook

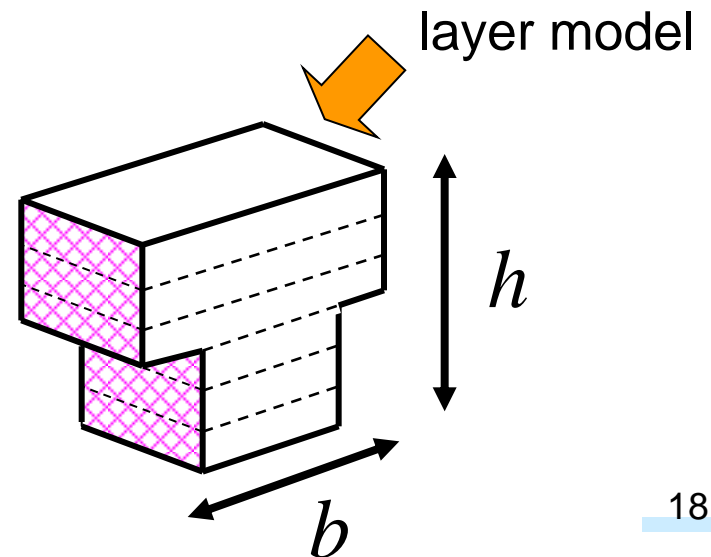
same model as used in load estimation



design variables

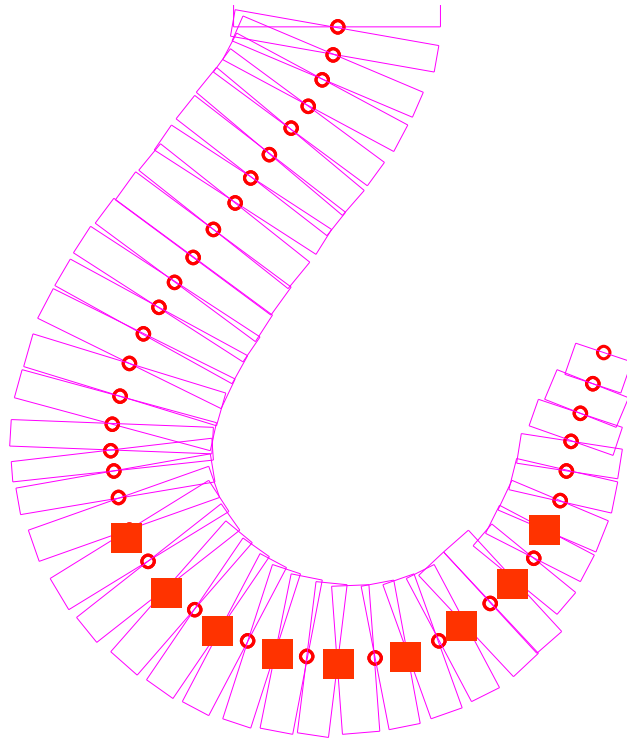
height  $h$

width  $b$



# Objective Function

design objective: **light weight**, **high stiffness**



■ : possible load applied points

criterion (1)

**structural weight**

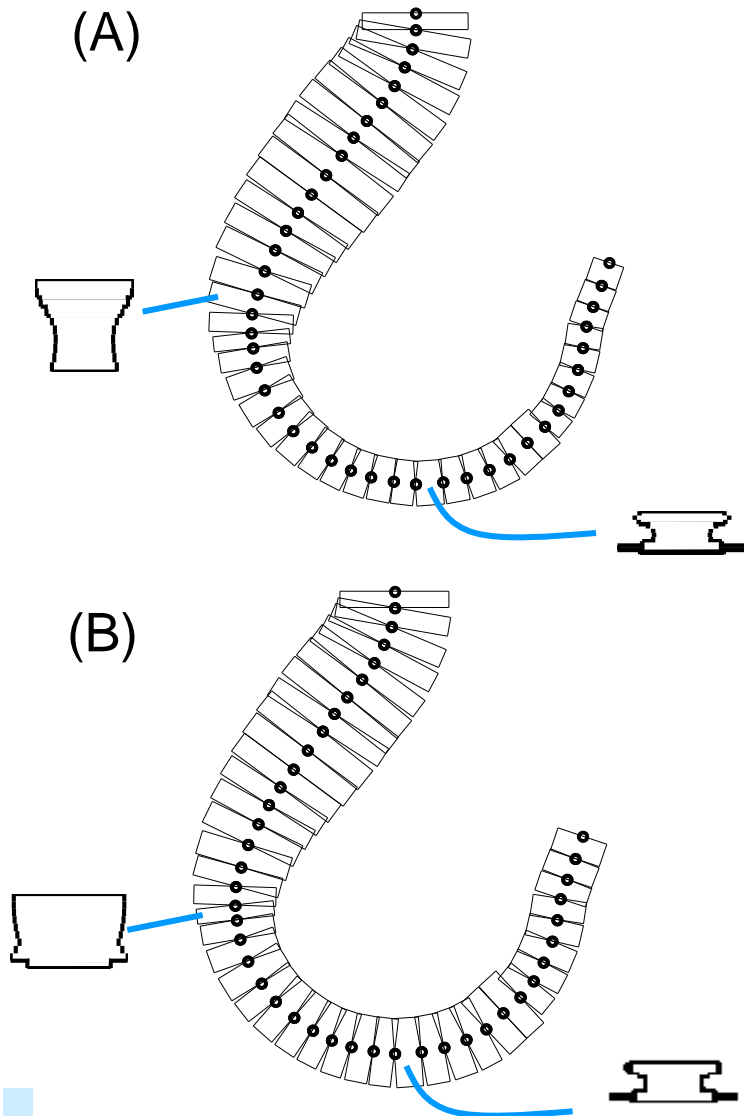
criterion (2)

**structural stiffness**

↳ ratio between load and displacement

( load vector is specified by estimation result of load applied point )

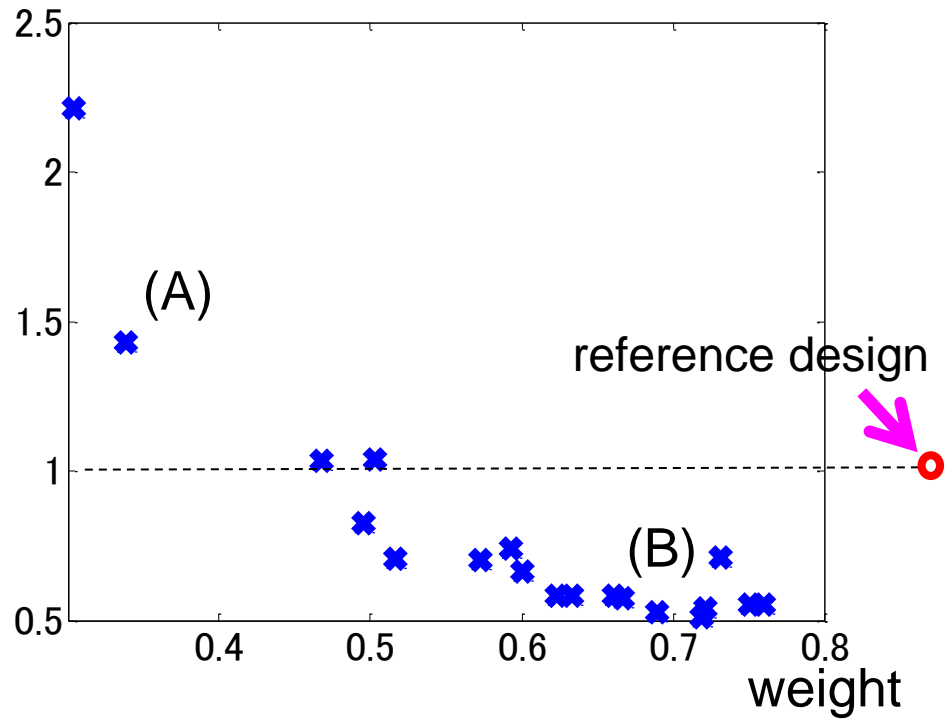
# Obtained Designs



stiffness

low

high



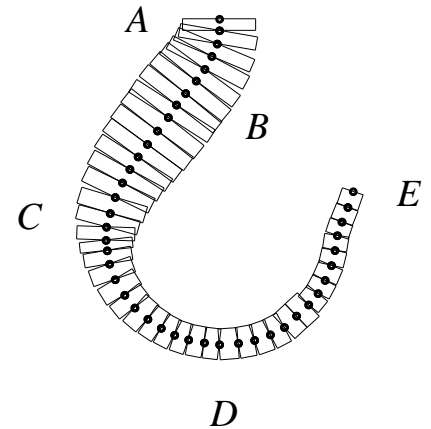
light

heavy

# Features of Obtained Design

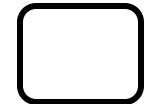
## □ hook shape

- hook shape becomes thinner toward the tip point “E” from the lowest center point “D”
- thickness of region around the point “B” is greater than any other region



## □ cross-sectional shape

- cross-sectional shape of the point “C” is rectangular
- at the point “D”, center part is thinner than both end side (upper and lower)



I-shape





# Conclusion

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## ★ load estimation


implement elasto-plastic analysis  
for construction of Load-Deformation database

- load position lies between lower center and tip-end
- load magnitude is four times larger than nominal load
- load direction is downward

## ★ shape design

formulate multi-objective optimization problem  
taking account of estimation results

- obtained hook shapes have a tapered shape
- cross-sectional shapes do not have “a T-shape”  
but have “a rectangular” or “an I-shape”



Questions are welcome.  
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# EM Algorithm

probability density function (PDF)

↳ **mixture Gaussian model**

$$P(\boldsymbol{x}) = \sum_{k=1}^K \pi_k N(\boldsymbol{x} | \boldsymbol{\mu}_k, \mathbf{V}_k), \quad N(\boldsymbol{x} | \boldsymbol{\mu}, \mathbf{V}) = \frac{1}{(2\pi)^{D/2} |\mathbf{V}|^{1/2}} \exp\left\{-\frac{(\boldsymbol{x} - \boldsymbol{\mu})^T \mathbf{V}^{-1} (\boldsymbol{x} - \boldsymbol{\mu})}{2}\right\},$$

## ★ EM algorithm

**Step1**

$$\gamma(z_{nk}) = \frac{\pi_k N(\boldsymbol{x}_n | \boldsymbol{\mu}_k, \mathbf{V}_k)}{\sum_{j=1}^K \pi_j N(\boldsymbol{x}_n | \boldsymbol{\mu}_j, \mathbf{V}_j)}$$

**Step2**

$$\boldsymbol{\mu}_k^{\text{new}} = \frac{1}{N_k} \sum_{n=1}^N \gamma(z_{nk}) \boldsymbol{x}_n$$
$$\mathbf{V}_k^{\text{new}} = \frac{1}{N_k} \sum_{n=1}^N \gamma(z_{nk}) (\boldsymbol{x}_n - \boldsymbol{\mu}_k^{\text{new}})(\boldsymbol{x}_n - \boldsymbol{\mu}_k^{\text{new}})^T$$

$$\pi_k^{\text{new}} = \frac{N_k}{N}$$

$\pi_k$  : mixture weight

$\boldsymbol{\mu}$  : mean

$\mathbf{V}$  : variance